

Prediction of turbidity using neural networks: application on chalk aquifer of Normandy (France)

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Yport cliff

Turbidity

Definition, origins and properties

- Ability of a liquid to disrupt a light beam.
- Turbidity essentially comes from two processes; the surface run-off or/and the underground matter resuspension.
- Could be an indicator of surface contaminations (fecal particles, phytosanitary products,...).
- Non linear response to rainfalls.

Yport localization



Normandie hydrogeological context



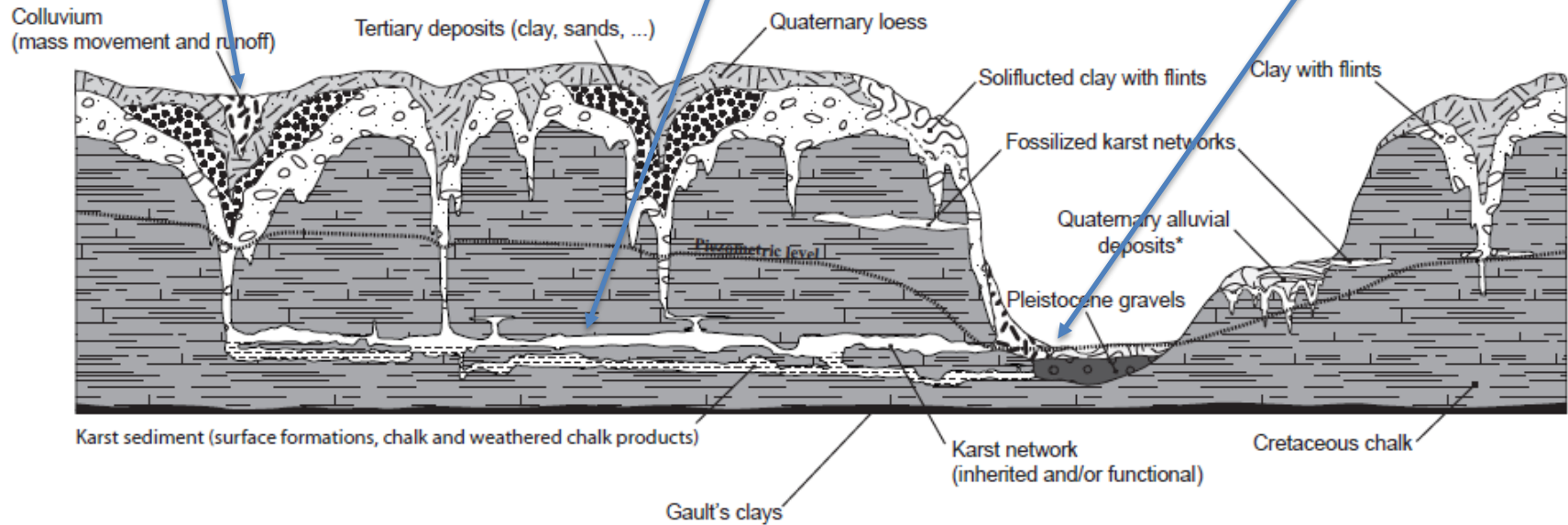
Bétoires



Karst duct



Yport fountain



Schematic cut of the superficial formation in the Seine Maritime (Chédeville, S. & al. 2014a)

Yport fresh water pumping well

Stakes

- Responsible for the half of Le Havre/Great Le Havre drinking water supplying (180,000 inhabitant)
- Regularly contaminated by turbid water (potability norms < 1 NTU)
- Risk of phytosanitary product contamination

Managers needs

- Forecast 12h and 24h ahead a 100NTU threshold overtaking.
- Water storage to avoid turbid water pumping
- Clean processing chain to maximize the filtration if pumping is necessary



100 NTU



Yport drinking water station

Database

6 rain gauges

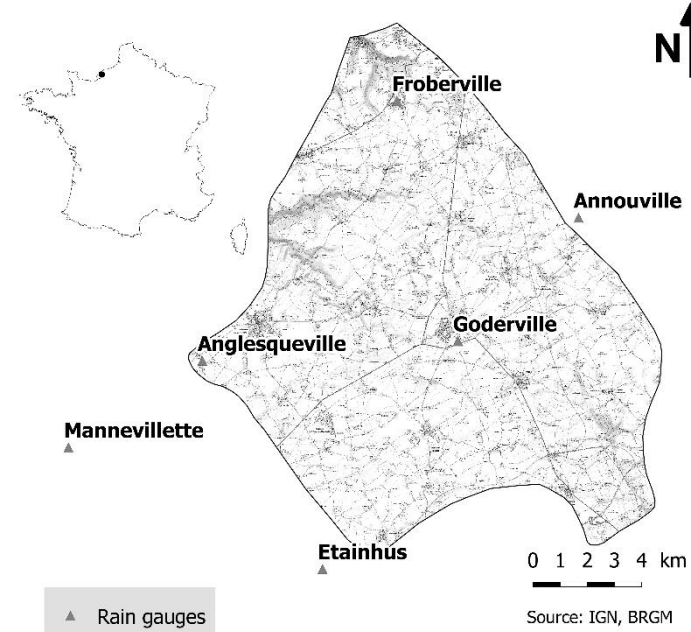
- Data since 2009 at hourly time step (with gaps)

1 turbidimeter

- At the input of the station : data since 1993 at hourly time step (with gaps)

Underground discharge cannot be measured

22 events selected



Event without turbidity peak

Event	Duration (hours)	Turbidity (NTU)		Rain (mm)
		Max	Min	Cumul
1	288	7.07	1	15.9
4	384	9.82	0.91	14.1
5	336	7.71	1.52	17.5
8	360	26.87	0.97	22.5
9	384	9	1.00	20.2
12	456	12	0.84	28.7
13	576	13	0.86	30.8
14	384	14	0.86	23.3
15	600	15	0.85	31.7
19	504	19	1.50	30.3
20	576	20	0.89	40.8
21	600	48.44	0.93	48.5

Event with turbidity peak

Event	Duration (hours)	Turbidity (NTU)		Rain (mm)
		Max	Min	Cumul
2	624	302.48	1.54	41.3
3	1008	135.03	0	26.7
6	720	245.38	1.53	42.0
7	744	84.67	0.05	19.2
10	576	256.15	0.92	24.9
11	744	307.89	0.87	54.8
16	648	405.25	0.81	53.8
17	744	157.45	0.49	50.7
18	744	86.67	2.18	42.8
22	623	53.91	0.80	44.2

Turbidity forecasting: state of the art

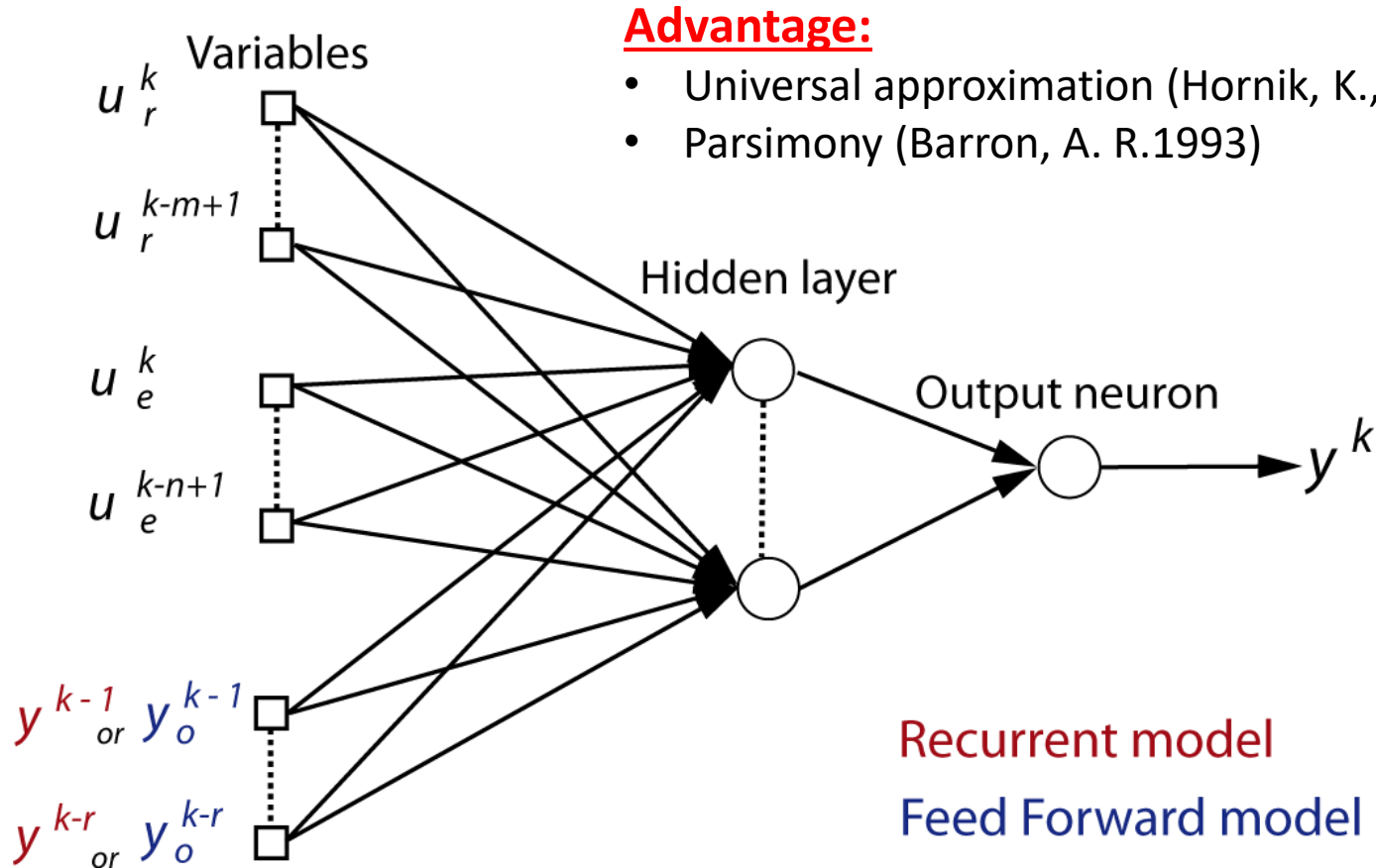
- Turbidity results from complex and difficult to observe processes
 - No physical model
 - Black box
- Discharge/Turbidity relation models
 - Neural network and particle swarm optimization with daily data (Houria, B & al 2014)
 - Neural network with hourly data (Mulia, I. E. & al. 2013)
- Rainfall/Turbidity relation models
 - Local logistic regression with monthly data (Towler ,E. & al 2010)
 - Adjust probabilistic distribution to daily data (Y. Tramblay. 2007)

Goals of the present study

Forecast turbidity using rainfall at 12h lead time

Neural network models

Multilayer perceptron architecture



u_r : Rainfalls

u_e : ETP

y : Turbidity

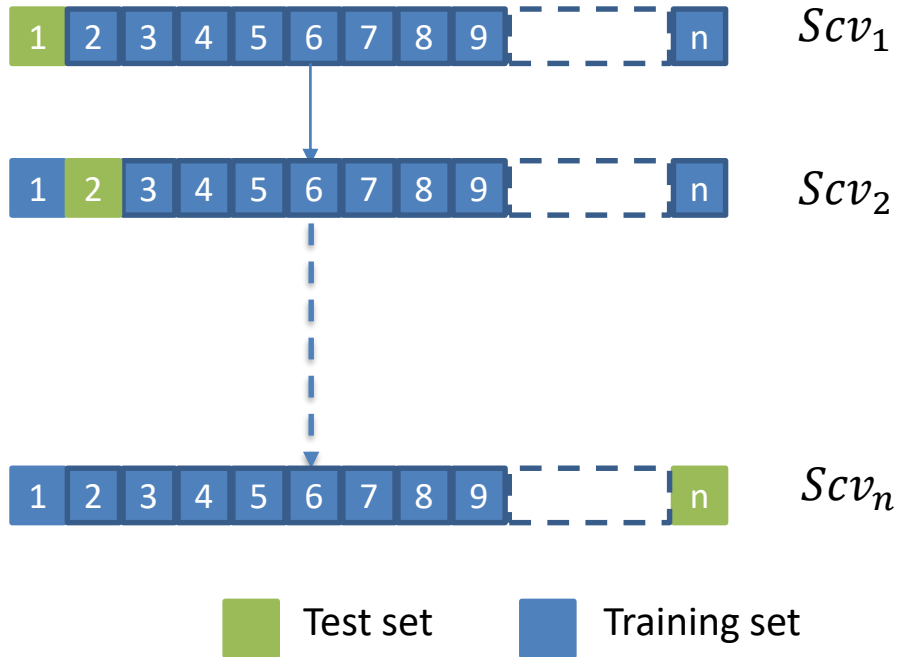
Limits:

- Bias-variance dilemma (Geman, S. & *al* 1992)
- Overfitting (Sjöberg, J., & *al* 1995)

Regularization methods

To deal with bias-variance dilemma

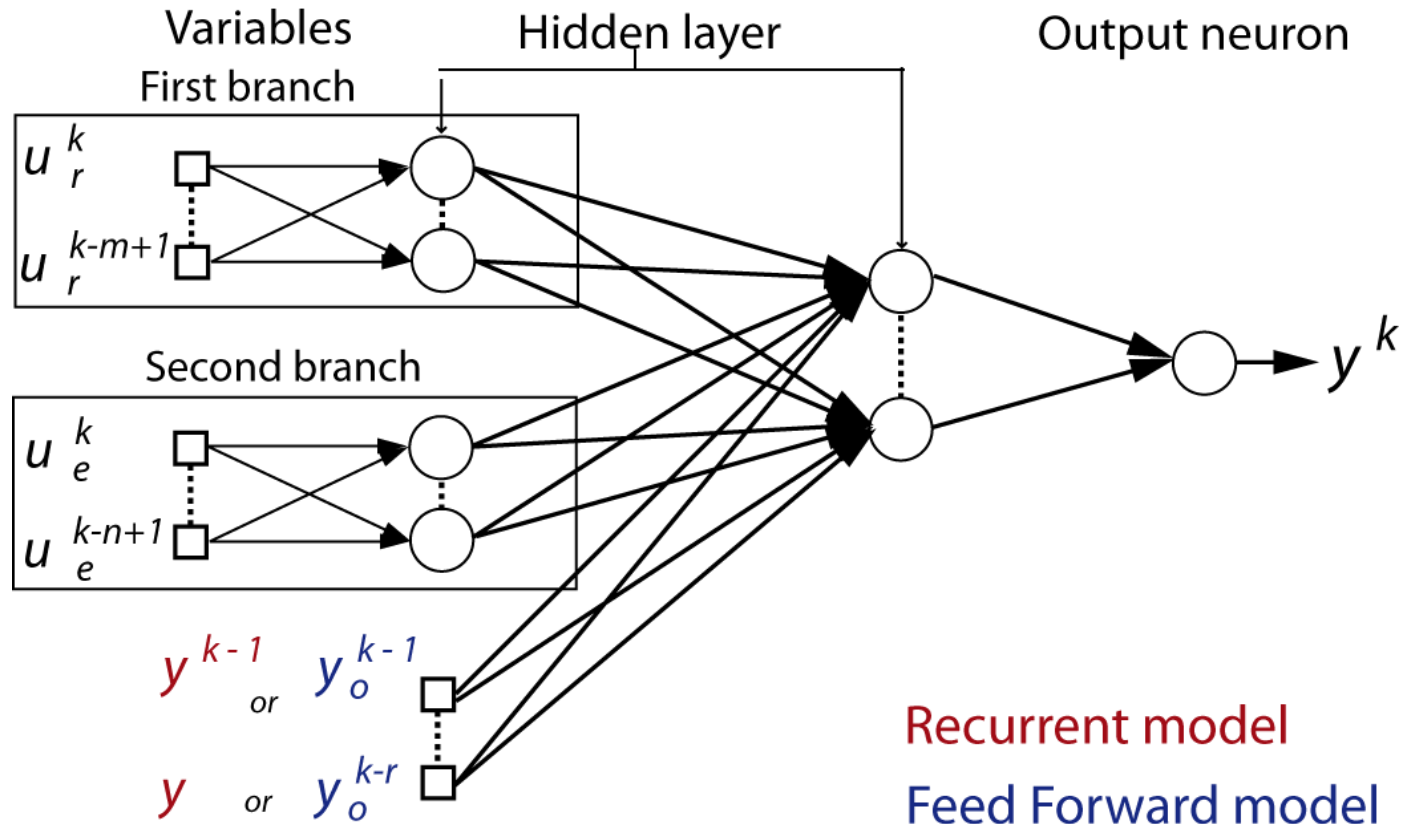
- Cross-validation (Stone, M. 1974)
- Early stopping (Morgan, N., & Boulard, H. 1989, Sjöberg, J., & al 1995).



$$Scv_{validation} = \frac{\sum_{i=1}^n Scv_i}{n}$$

Neural network models

Multilayer perceptron based architecture:
Two-branches model (Johannet, A., & *al* 2008)



u_r : Rainfalls

u_e : ETP

y : Turbidity

Designed models

6 rain gauges

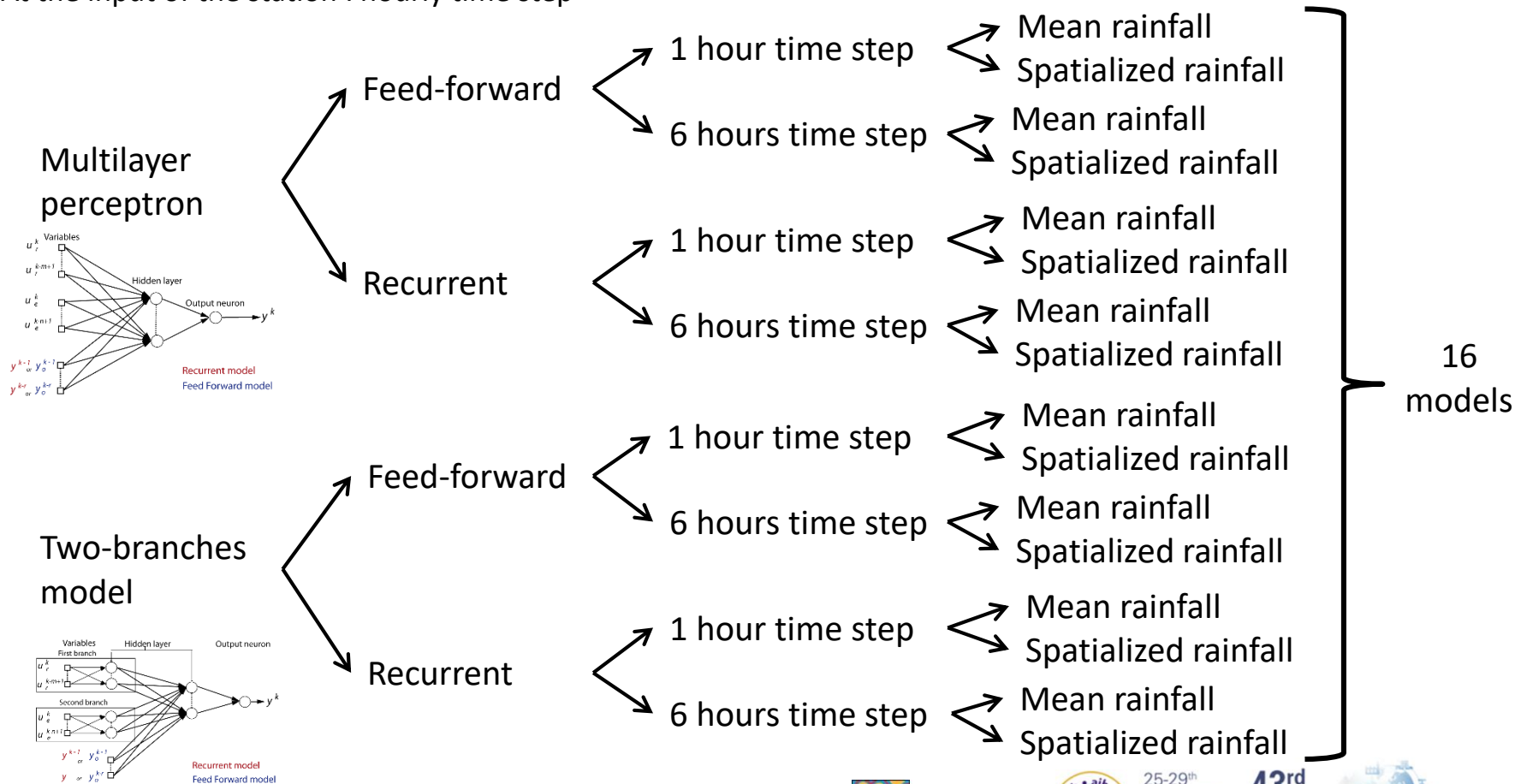
- Data at hourly time step (with gaps)

1 turbidimeter

- At the input of the station : hourly time step

Goal of the models:

- Complexity decreasing by six hours sampling
- Evaluation of the spatialization of rainfalls interest



Quality criteria

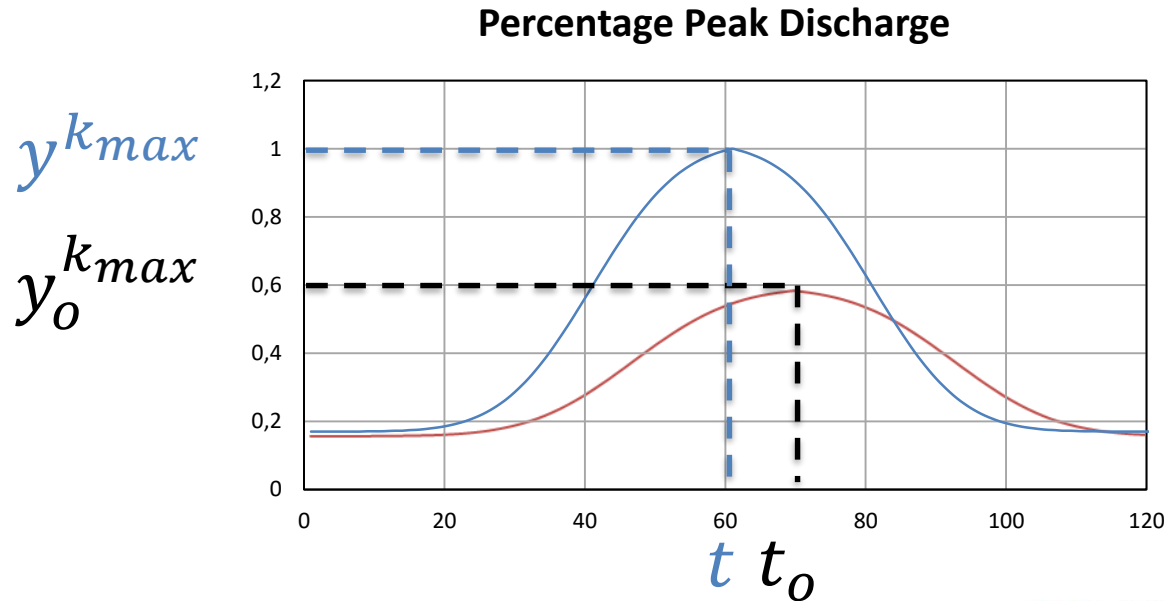
Percentage of the Peak Discharge and the Peak Delay

$$P_{PD} = 100 \frac{y^{k_{\max}}}{y_o^{k_{\max}}}$$

PPD (Percentage of the
Peak Discharge)
(Artigue G., & al (2012))

$$P_D = t - t_o$$

PD (Peak Delay)

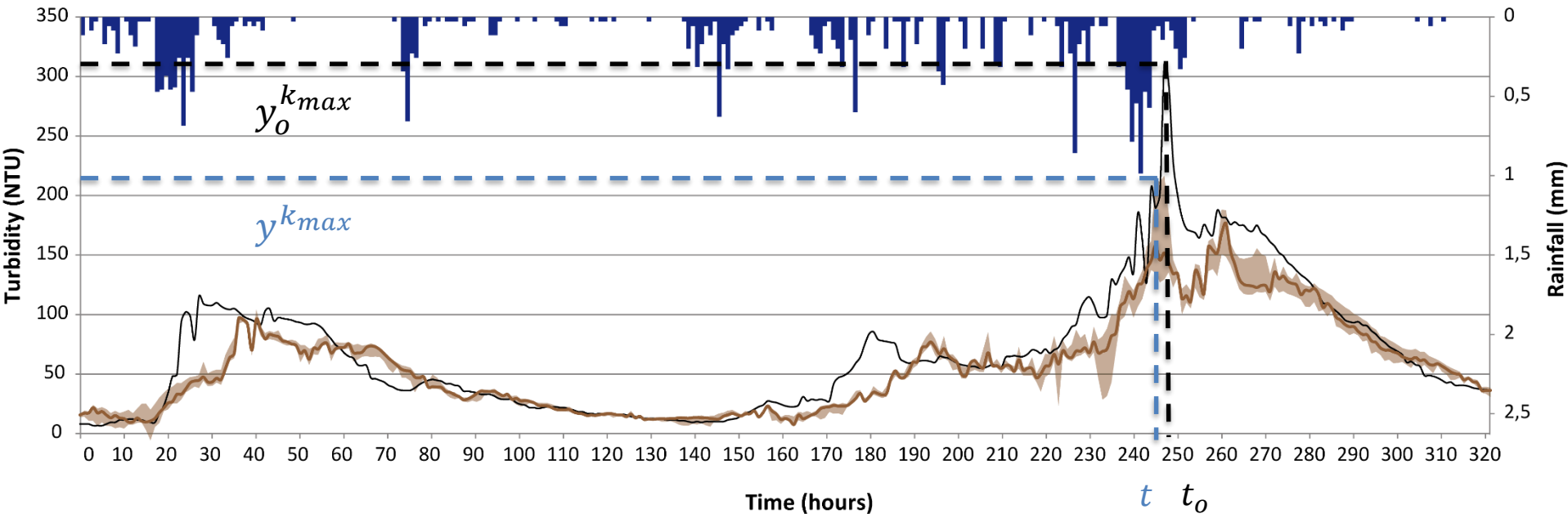


Results

Illustration on test event n°11

(01/12/2011 to 30/12/2011)

Multi-layer perceptron feed-forward model



- Rainfall
- Observed turbidity
- Forecasted turbidity
- Uncertainty

$$P_{PD} = 59 \%$$

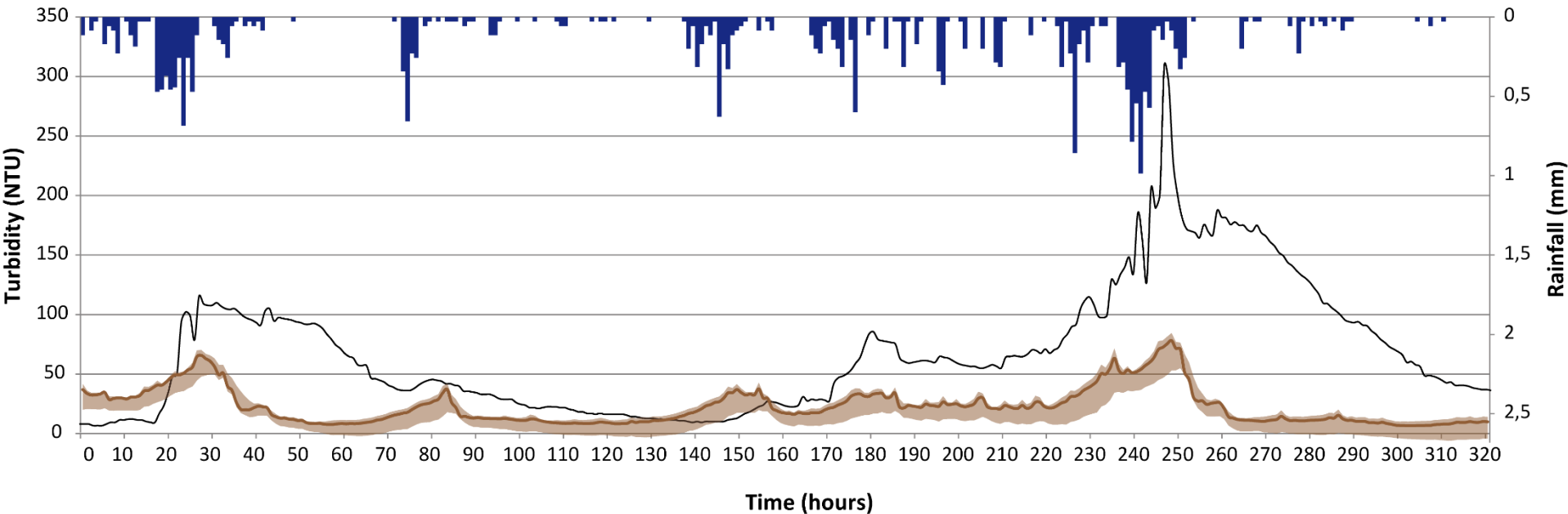
$$P_p = 8 \text{ h}$$

Results

Illustration on test event n°11

(01/12/2011 to 30/12/2011)

Multi-layer perceptron recurrent model



- Rainfall
- Observed turbidity
- Forecasted turbidity
- Uncertainty

$$P_{PD} = 25 \%$$

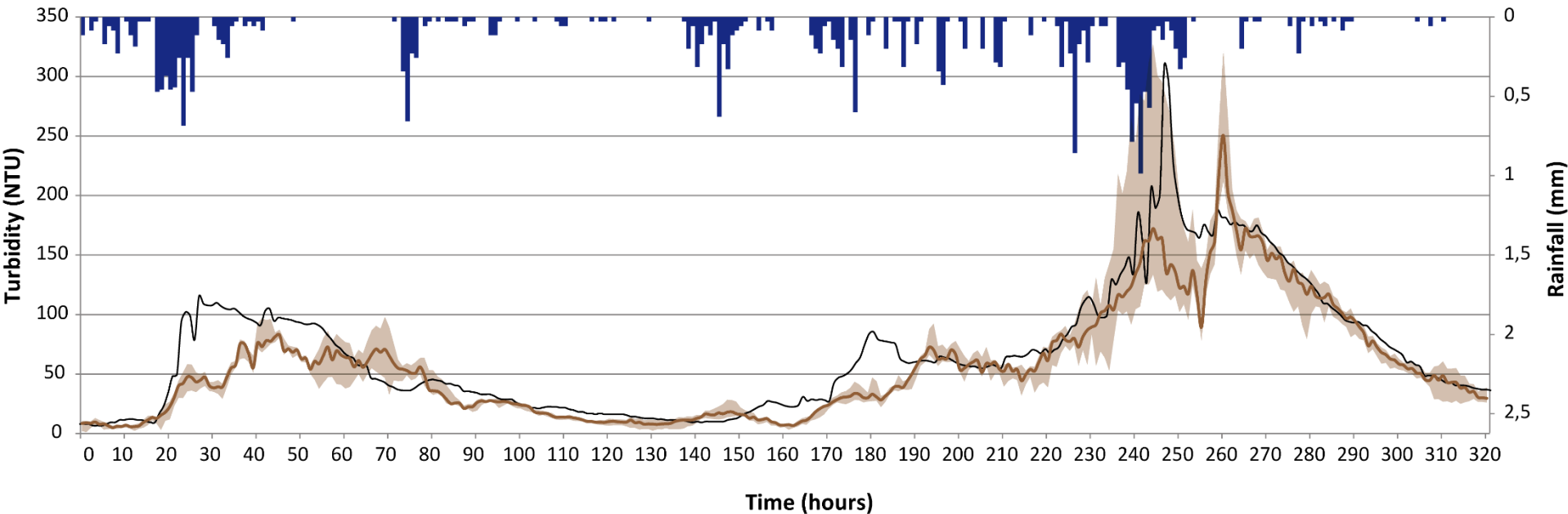
$$P_p = 3 \text{ h}$$

Results

Illustration on test event n°11

(01/12/2011 to 30/12/2011)

Two branches feed-forward model



- Rainfall
- Observed turbidity
- Forecasted turbidity
- Uncertainty

$$P_{PD} = 80 \%$$

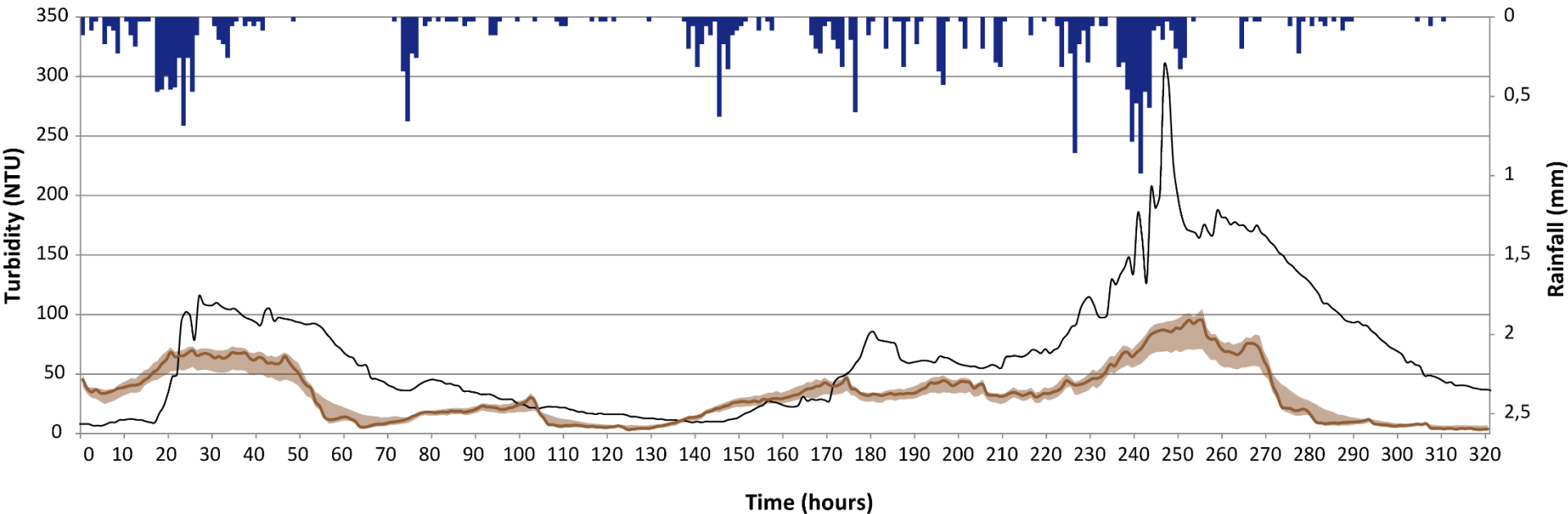
$$P_p = 15 \text{ h}$$

Results

Illustration on test event n°11

(01/12/2011 to 30/12/2011)

Tow branches recurrent model



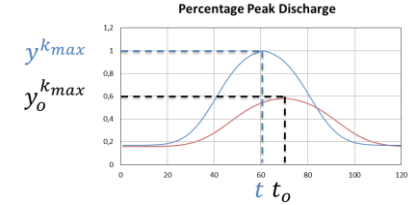
- Rainfall
- Observed turbidity
- Forecasted turbidity
- Uncertainty

$$P_{PD} = 28 \%$$

$$P_p = 10h$$

Results: Model with hourly data and mean rainfall

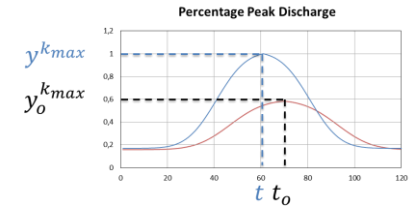
Cross test



	Two branches feed-forward		Two branches recurrent		MLP feed-forward		MLP recurrent	
	P _{PD}	Peak delay (h)	P _{PD}	Peak delay (h)	P _{PD}	Peak delay (h)	P _{PD}	Peak delay (h)
T ₂	79.95	<u>4</u>	38.01	18	<u>80.62</u>	19	39.58	21
T ₃	112.95	<u>4</u>	60.99	15	<u>108.67</u>	4	70.63	3
T ₆	217.41	<u>8</u>	79.97	10	<u>93.30</u>	14	69.70	10.50
T ₇	Stop set		75.06	<u>2</u>	<u>82.89</u>	14	75.44	3
T ₁₀	<u>86.04</u>	7	40.92	<u>4</u>	50.38	14	Stop set	
T ₁₁	<u>80.36</u>	15	28.48	10	59.46	8	25.69	<u>3</u>
T ₁₆	<u>106.39</u>	<u>2</u>	Stop set		65.52	14	44.16	10
T ₁₇	<u>105.55</u>	<u>5</u>	87.55	101	Stop set		50.21	9
T ₁₈	<u>98.17</u>	97	152.86	3	89.84	102	79.53	<u>0</u>
T ₂₂	<u>143.54</u>	<u>3</u>	152.33	14	169.18	4	149.17	6
Median	<u>105</u>	<u>5</u>	75	10	83	14	70	6

Results: Model with hourly data and mean rainfall

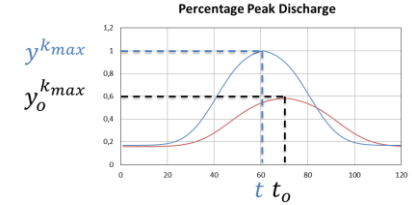
Cross test



	Two branches feed-forward		Two branches recurrent		MLP feed-forward		MLP recurrent	
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Results: Model with hourly data and spatialized rainfalls

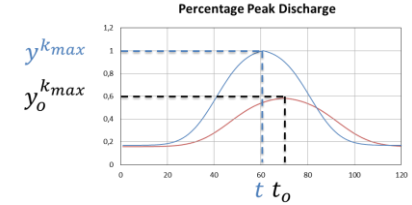
Cross test



	Two branches feed-forward		Two branches recurrent		MLP feed-forward		MLP recurrent	
	P _{PD}	Peak delay (h)	P _{PD}	Peak delay (h)	P _{PD}	Peak delay (h)	P _{PD}	Peak delay (h)
T ₂	128,2	17	36,4	27	<u>89,6</u>	<u>16</u>	32,2	20
T ₃	<u>101,6</u>	4	80,3	84	105,0	8	77,2	<u>3</u>
T ₆	173,5	11	56,3	13	<u>117,0</u>	<u>11</u>	46,4	12
T ₇	Stop set		61,7	8	80,5	14	<u>81,5</u>	<u>4</u>
T ₁₀	<u>85,0</u>	9	63,7	<u>3</u>	72,6	14	Stop set	
T ₁₁	65,7	11	31,0	11	<u>67,6</u>	14	28,9	<u>3</u>
T ₁₆	<u>219,5</u>	<u>9</u>	Stop set		61,5	15	40,1	12
T ₁₇	<u>94,5</u>	<u>7</u>	61,1	8	Stop set		49,3	11
T ₁₈	135,0	103	<u>93,1</u>	<u>13</u>	115,2	14	83,0	69
T ₂₂	229,8	10	181,5	8	<u>128,5</u>	10	172,3	<u>7</u>
Median	137,0	20	73,9	19	<u>94,6</u>	<u>13</u>	67,9	15

Results: Model with hourly data and **spatialized rainfalls**

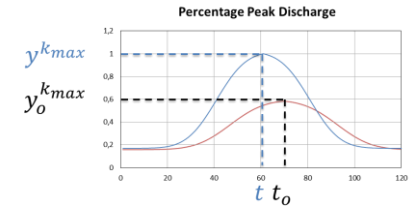
Cross test



	Two branches feed-forward		Two branches recurrent		MLP feed-forward		MLP recurrent	
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Results: Model with six hours sampling data and mean rainfall

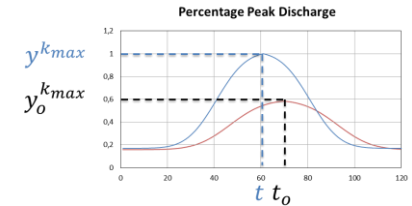
Cross test



	Two branches feed-forward		Two branches recurrent		MLP feed-forward		MLP recurrent	
	P _{PD}	Peak delay (6h)	P _{PD}	Peak delay (6h)	P _{PD}	Peak delay (6h)	P _{PD}	Peak delay (6h)
T ₂	<u>147,6</u>	4	39,0	<u>3</u>	67,9	<u>3</u>	41,2	4
T ₃	110,9	<u>2</u>	68,3	3	<u>96,3</u>	3	78,2	<u>2</u>
T ₆	242,5	3	81,2	4	<u>117,3</u>	3	71,0	<u>2</u>
T ₇	Stop set		75,0	2	<u>81</u>	4	66,6	<u>1</u>
T ₁₀	<u>75,1</u>	3	48,4	<u>2</u>	60,1	4	Stop set	
T ₁₁	62,8	3	28,3	<u>2</u>	<u>65,6</u>	4	34,3	<u>2</u>
T ₁₆	<u>132,0</u>	<u>3</u>	Stop set		62,5	4	35,1	4
T ₁₇	<u>121,6</u>	<u>2</u>	53,9	2	Stop set		43,8	2
T ₁₈	<u>92,4</u>	<u>2</u>	75,2	5	91,3	4	82,5	7
T ₂₂	187,3	3	161,8	2	<u>148,6</u>	<u>2</u>	166,8	3
Median	130,3	3	70,1	3	<u>87,8</u>	<u>3</u>	68,8	3

Results: Model with six hours sampling data and mean rainfall

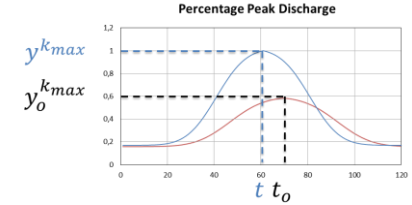
Cross test



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Results: Model with six hours sampling data and **spatialized rainfall**

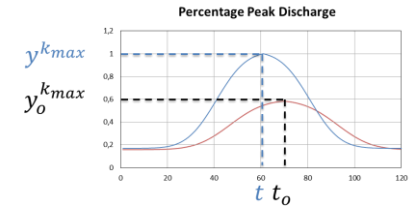
Cross test



	Two branches feed-forward		Two branches recurrent		MLP feed-forward		MLP recurrent	
	P _{PD}	Peak delay (6h)	P _{PD}	Peak delay (6h)	P _{PD}	Peak delay (6h)	P _{PD}	Peak delay (6h)
T ₂	186,4	6	38,2	6	<u>67,0</u>	9	41,1	<u>3</u>
T ₃	114,9	2	41,4	3	<u>93,9</u>	3	63,5	<u>1</u>
T ₆	196,9	4	60,9	3	<u>85,2</u>	<u>3</u>	59,7	3
T ₇	Stop set		<u>73,4</u>	<u>2</u>	63	5	52,1	6
T ₁₀	<u>116,2</u>	<u>3</u>	56,5	<u>2</u>	65,4	4	Stop set	
T ₁₁	<u>66,3</u>	<u>3</u>	33,7	<u>3</u>	67,9	4	30,8	<u>3</u>
T ₁₆	<u>250,1</u>	<u>2</u>	Stop set		59,8	4	40,4	3
T ₁₇	<u>120,1</u>	2	56,3	3	Stop set		48,9	<u>1</u>
T ₁₈	89,2	5	113,0	<u>4</u>	<u>105,3</u>	17	93,5	5
T ₂₂	292,7	3	192,8	2	89,3	3	<u>115,1</u>	<u>2</u>
Median	159,2	3	<u>74,0</u>	<u>3</u>	77,4	6	60,6	3

Results: Model with six hours sampling data and **spatialized rainfall**

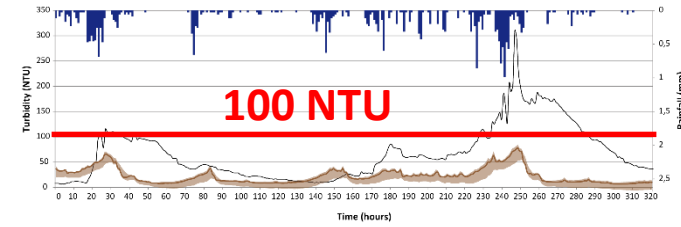
Cross test



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Results: Model with hourly data and mean rainfall

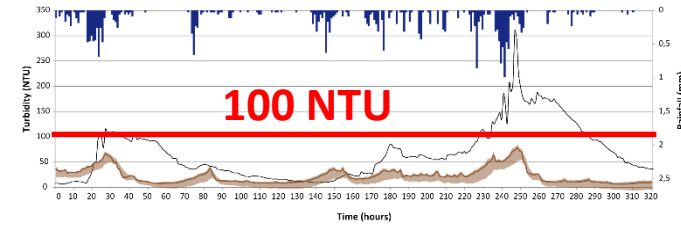
Cross test (100 NTU threshold overtaking)



	Two branches feed-forward				Two branches recurrent				MLP feed-forward				MLP recurrent			
	F _p	F _n	d _r (h)	d _d (h)	F _p	F _n	d _r (h)	d _d (h)	F _p	F _n	d _r (h)	d _d (h)	F _p	F _n	d _r (h)	d _d (h)
T ₂	0	0	6	11	0	0	6	-76	<u>0</u>	<u>0</u>	<u>6</u>	<u>8</u>	0	0	6	-53
T ₃	<u>1</u>	<u>0</u>	<u>0</u>	<u>3</u>	1	0	-11	-4	1	0	7	4	0	0	0	-22
T ₆	0	0	-4	10	0	0	-5	6	0	0	-4	9	<u>0</u>	<u>0</u>	<u>-4</u>	<u>4</u>
T ₇	Stop set				X	X	X	X	X	X	X	X	X	X	X	X
T ₁₀	0	1	-2	10	<u>0</u>	<u>0</u>	<u>-1</u>	<u>9</u>	0	0	-9	11	Stop set			
T ₁₁	0	1	3	6	0	1	-17	-31	<u>0</u>	<u>0</u>	<u>-12 / 8</u>	<u>-3 / 4</u>	0	2	X	X
T ₁₆	0	0	14	18	Stop set				<u>0</u>	<u>0</u>	<u>1</u>	<u>12</u>	0	0	6	-19
T ₁₇	1	1	X	X	0	1	X	X	Stop set				0	1	X	X
T ₁₈	<u>0</u>	<u>0</u>	<u>X</u>	<u>X</u>	<u>0</u>	<u>0</u>	<u>X</u>	<u>X</u>	<u>0</u>	<u>0</u>	<u>X</u>	<u>X</u>	1	0	X	X
T ₂₂	1	0	X	X	<u>0</u>	<u>0</u>	<u>X</u>	<u>X</u>	<u>0</u>	<u>0</u>	<u>X</u>	<u>X</u>	1	0	X	X
Median	0.2	0.3	1.5	10	<u>0.1</u>	0.3	-5	<u>-4</u>	0.2	<u>0</u>	<u>-1.5</u>	8	0.3	0.4	3	-20

Results: Model with hourly data and mean rainfall

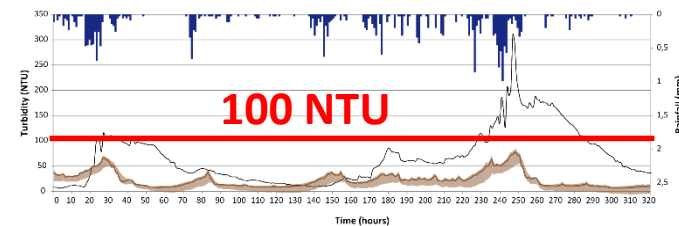
Cross test (100 NTU threshold overtaking)



	Two branches feed-forward				Two branches recurrent				MLP feed-forward				MLP recurrent			
	F _p	F _n	d _r (h)	d _d (h)	F _p	F _n	d _r (h)	d _d (h)	F _p	F _n	d _r (h)	d _d (h)	F _p	F _n	d _r (h)	d _d (h)
T ₂	0	0	6	11	0	0	6	-76	<u>0</u>	<u>0</u>	<u>6</u>	<u>8</u>	0	0	6	-53
T ₃	<u>1</u>	<u>0</u>	<u>0</u>	<u>3</u>	1	0	-11	-4	1	0	7	4	0	0	0	-22
T ₆	0	0	-4	10	0	0	-5	6	0	0	-4	9	<u>0</u>	<u>0</u>	<u>-4</u>	<u>4</u>
T ₇	Stop set				X	X	X	X	X	X	X	X	X	X	X	X
T ₁₀	0	1	-2	10	<u>0</u>	<u>0</u>	<u>-1</u>	<u>9</u>	0	0	-9	11	Stop set			
T ₁₁	0	1	3	6	0	1	-17	-31	<u>0</u>	<u>0</u>	<u>-12 / 8</u>	<u>-3 / 4</u>	0	2	X	X
T ₁₆	0	0	14	18	Stop set				<u>0</u>	<u>0</u>	<u>1</u>	<u>12</u>	0	0	6	-19
T ₁₇	1	1	X	X	0	1	X	X	Stop set				0	1	X	X
T ₁₈	<u>0</u>	<u>0</u>	<u>X</u>	<u>X</u>	<u>0</u>	<u>0</u>	<u>X</u>	<u>X</u>	<u>0</u>	<u>0</u>	<u>X</u>	<u>X</u>	1	0	X	X
T ₂₂	1	0	X	X	<u>0</u>	<u>0</u>	<u>X</u>	<u>X</u>	<u>0</u>	<u>0</u>	<u>X</u>	<u>X</u>	1	0	X	X
Median	0.2	0.3	1.5	10	<u>0.1</u>	0.3	-5	<u>-4</u>	0.2	<u>0</u>	<u>-1.5</u>	8	0.3	0.4	3	-20

Results: Model with hourly data and spatialized rainfalls

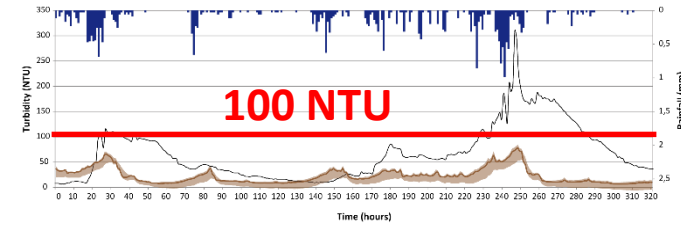
Cross test (100 NTU threshold overtaking)



	Two branches feed-forward				Two branches recurrent				MLP feed-forward				MLP recurrent			
	F _p	F _n	d _r (h)	d _d (h)	F _p	F _n	d _r (h)	d _d (h)	F _p	F _n	d _r (h)	d _d (h)	F _p	F _n	d _r (h)	d _d (h)
T ₂	0	0	-3	-8	0	0	-9	-32	0	0	-5	8	<u>0</u>	<u>0</u>	<u>0</u>	<u>-88</u>
T ₃	0	0	6	-3	1	1	X	X	<u>1</u>	<u>0</u>	<u>4</u>	<u>-24</u>	<u>1</u>	<u>0</u>	<u>4</u>	<u>-24</u>
T ₆	0	0	4	-10	1	0	4	-9	<u>1</u>	<u>0</u>	<u>-1</u>	<u>-15</u>	1	0	1	-15
T ₇	Stop set				0	0	X	X	0	0	X	X	0	0	X	X
T ₁₀	0	0	-4	-11	<u>0</u>	<u>0</u>	<u>-3</u>	<u>17</u>	0	0	3	17	Stop set			
T ₁₁	<u>0</u>	<u>0</u>	<u>7/9</u>	<u>-1/-1</u>	0	1	X/-25	X/-20	0	2	X	X	0	2	X	X
T ₁₆	<u>0</u>	<u>0</u>	<u>-6</u>	<u>-13</u>	Stop set				0	0	-6	-19	0	0	-6	-19
T ₁₇	0	2	13	-13	<u>0</u>	<u>2</u>	<u>10</u>	<u>-8</u>	Stop set				0	3	X	X
T ₁₈	1	0	X	X	<u>0</u>	<u>0</u>	<u>X</u>	<u>X</u>	<u>0</u>	<u>0</u>	<u>X</u>	<u>X</u>	<u>0</u>	<u>0</u>	<u>X</u>	<u>X</u>
T ₂₂	2	0	X	X	<u>1</u>	<u>0</u>	<u>X</u>	<u>X</u>	<u>1</u>	<u>0</u>	<u>X</u>	<u>X</u>	<u>1</u>	<u>0</u>	<u>X</u>	<u>X</u>
Median	0	0	5	-9	0	0	-3	-9	<u>0</u>	<u>0</u>	<u>-1</u>	<u>-15</u>	0	1	1	-22

Results: Model with hourly data and spatialized rainfalls

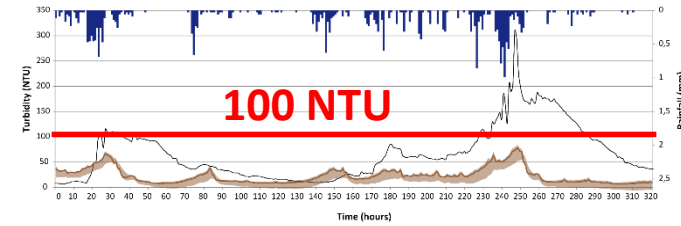
Cross test (100 NTU threshold overtaking)



	Two branches feed-forward				Two branches recurrent				MLP feed-forward				MLP recurrent			
	F _p	F _n	d _r (h)	d _d (h)	F _p	F _n	d _r (h)	d _d (h)	F _p	F _n	d _r (h)	d _d (h)	F _p	F _n	d _r (h)	d _d (h)
T ₂	0	0	-3	-8	0	0	-9	-32	0	0	-5	8	<u>0</u>	<u>0</u>	<u>0</u>	<u>-88</u>
T ₃	0	0	6	-3	1	1	X	X	<u>1</u>	<u>0</u>	<u>4</u>	<u>-24</u>	<u>1</u>	<u>0</u>	<u>4</u>	<u>-24</u>
T ₆	0	0	4	-10	1	0	4	-9	<u>1</u>	<u>0</u>	<u>-1</u>	<u>-15</u>	1	0	1	-15
T ₇	Stop set				0	0	X	X	0	0	X	X	0	0	X	X
T ₁₀	0	0	-4	-11	<u>0</u>	<u>0</u>	<u>-3</u>	<u>17</u>	0	0	3	17	Stop set			
T ₁₁	<u>0</u>	<u>0</u>	<u>7/9</u>	<u>-1/-1</u>	0	1	X/-25	X/-20	0	2	X	X	0	2	X	X
T ₁₆	<u>0</u>	<u>0</u>	<u>-6</u>	<u>-13</u>	Stop set				0	0	-6	-19	0	0	-6	-19
T ₁₇	0	2	13	-13	<u>0</u>	<u>2</u>	<u>10</u>	<u>-8</u>	Stop set				0	3	X	X
T ₁₈	1	0	X	X	<u>0</u>	<u>0</u>	<u>X</u>	<u>X</u>	<u>0</u>	<u>0</u>	<u>X</u>	<u>X</u>	<u>0</u>	<u>0</u>	<u>X</u>	<u>X</u>
T ₂₂	2	0	X	X	<u>1</u>	<u>0</u>	<u>X</u>	<u>X</u>	<u>1</u>	<u>0</u>	<u>X</u>	<u>X</u>	<u>1</u>	<u>0</u>	<u>X</u>	<u>X</u>
Median	0	0	5	-9	0	0	-3	-9	<u>0</u>	<u>0</u>	<u>-1</u>	<u>-15</u>	0	1	1	-22

Results: Model with six hours sampling data and mean rainfall

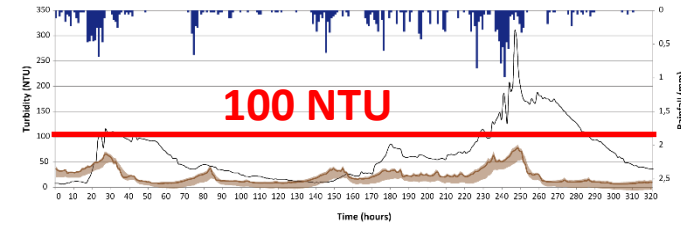
Cross test (100 NTU threshold overtaking)



	Two branches feed-forward				Two branches recurrent				MLP feed-forward				MLP recurrent			
	F _p	F _n	d _r (6h)	d _d (6h)	F _p	F _n	d _r (6h)	d _d (6h)	F _p	F _n	d _r (6h)	d _d (6h)	F _p	F _n	d _r (6h)	d _d (6h)
T ₂	0	0	0	3	0	0	0	-10	0	0	0	2	<u>0</u>	<u>0</u>	<u>0</u>	<u>-6</u>
T ₃	1	0	0	0	1	0	1	-2	1	0	0	0	<u>0</u>	<u>0</u>	<u>0</u>	<u>-4</u>
T ₆	<u>0</u>	<u>0</u>	<u>1</u>	<u>1</u>	0	0	2	1	0	0	2	1	0	0	1	-2
T ₇	Stop set				0	0	X	X	0	0	X	X	0	0	X	X
T ₁₀	0	0	3	3	<u>0</u>	<u>0</u>	<u>1</u>	<u>2</u>	0	0	1	3	Stop set			
T ₁₁	<u>0</u>	<u>0</u>	<u>2/1</u>	<u>1/1</u>	0	2	X	X	0	0	3/3	0/1	0	1	X/3	X/-7
T ₁₆	0	0	-1	3	Stop set				0	0	1	3	<u>0</u>	<u>0</u>	<u>0</u>	<u>4</u>
T ₁₇	<u>0</u>	<u>2</u>	<u>3</u>	<u>3</u>	0	2	5	1	Stop set				0	3	X	X
T ₁₈	0	0	X	X	0	0	X	X	0	0	X	X	0	0	X	X
T ₂₂	1	0	X	X	<u>0</u>	<u>0</u>	<u>X</u>	<u>X</u>	<u>0</u>	<u>0</u>	<u>X</u>	<u>X</u>	<u>0</u>	<u>0</u>	<u>X</u>	<u>X</u>
Median	0	0	2	2	0	0	1	1	0	0	0	1	<u>0</u>	<u>0</u>	<u>0</u>	<u>-4</u>

Results: Model with six hours sampling data and mean rainfall

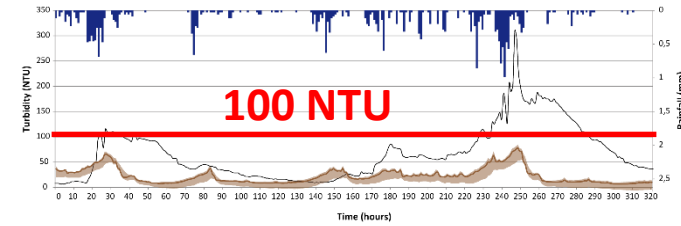
Cross test (100 NTU threshold overtaking)



	Two branches feed-forward				Two branches recurrent				MLP feed-forward				MLP recurrent			
	F _p	F _n	d _r (6h)	d _d (6h)	F _p	F _n	d _r (6h)	d _d (6h)	F _p	F _n	d _r (6h)	d _d (6h)	F _p	F _n	d _r (6h)	d _d (6h)
T ₂	0	0	0	3	0	0	0	-10	0	0	0	2	<u>0</u>	<u>0</u>	<u>0</u>	<u>-6</u>
T ₃	1	0	0	0	1	0	1	-2	1	0	0	0	<u>0</u>	<u>0</u>	<u>0</u>	<u>-4</u>
T ₆	<u>0</u>	<u>0</u>	<u>1</u>	<u>1</u>	0	0	2	1	0	0	2	1	0	0	1	-2
T ₇	Stop set				0	0	X	X	0	0	X	X	0	0	X	X
T ₁₀	0	0	3	3	<u>0</u>	<u>0</u>	<u>1</u>	<u>2</u>	0	0	1	3	Stop set			
T ₁₁	<u>0</u>	<u>0</u>	<u>2/1</u>	<u>1/1</u>	0	2	X	X	0	0	3/3	0/1	0	1	X/3	X/-7
T ₁₆	0	0	-1	3	Stop set				0	0	1	3	<u>0</u>	<u>0</u>	<u>0</u>	<u>4</u>
T ₁₇	<u>0</u>	<u>2</u>	<u>3</u>	<u>3</u>	0	2	5	1	Stop set				0	3	X	X
T ₁₈	0	0	X	X	0	0	X	X	0	0	X	X	0	0	X	X
T ₂₂	1	0	X	X	<u>0</u>	<u>0</u>	<u>X</u>	<u>X</u>	<u>0</u>	<u>0</u>	<u>X</u>	<u>X</u>	<u>0</u>	<u>0</u>	<u>X</u>	<u>X</u>
Median	0	0	2	2	0	0	1	1	0	0	0	1	<u>0</u>	<u>0</u>	<u>0</u>	<u>-4</u>

Results: Model with six hours sampling data and **spatialized rainfall**

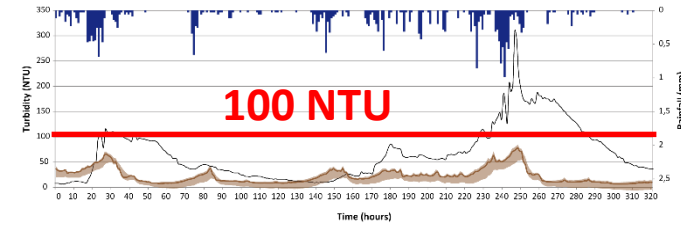
Cross test (100 NTU threshold overtaking)



	Two branches feed-forward				Two branches recurrent				MLP feed-forward				MLP recurrent			
	F _p	F _n	d _r (6h)	d _d (6h)	F _p	F _n	d _r (6h)	d _d (6h)	F _p	F _n	d _r (6h)	d _d (6h)	F _p	F _n	d _r (6h)	d _d (6h)
T ₂	0	0	-3	2	0	0	3	-3	0	0	2	2	<u>0</u>	<u>0</u>	<u>0</u>	<u>-12</u>
T ₃	<u>0</u>	<u>0</u>	<u>0</u>	<u>0</u>	0	0	1	-2	0	0	1	0	0	1	X	X
T ₆	<u>1</u>	<u>0</u>	<u>-1</u>	<u>0</u>	1	0	1	-1	0	0	3	-1	0	0	2	-2
T ₇	Stop set				0	0	X	X	0	0	X	X	0	0	X	X
T ₁₀	0	0	-1	3	<u>0</u>	<u>0</u>	<u>0</u>	<u>4</u>	0	0	3	3	Stop set			
T ₁₁	1	0	-1/2	-1/1	<u>0</u>	<u>0</u>	<u>0/3</u>	<u>-3/-2</u>	0	0	-2/-3	-1/1	0	1	-1/X	-1/X
T ₁₆	0	0	-1	2	Stop set				<u>0</u>	<u>0</u>	<u>0</u>	<u>1</u>	0	0	1	1
T ₁₇	<u>1</u>	<u>1</u>	<u>2</u>	<u>3</u>	0	3	X	X	Stop set				1	3	X	X
T ₁₈	<u>0</u>	<u>0</u>	<u>X</u>	<u>X</u>	2	0	X	X	<u>0</u>	<u>0</u>	<u>X</u>	<u>X</u>	<u>0</u>	<u>0</u>	<u>X</u>	<u>X</u>
T ₂₂	2	0	X	X	2	0	X	X	<u>0</u>	<u>0</u>	<u>X</u>	<u>X</u>	<u>0</u>	<u>0</u>	<u>X</u>	<u>X</u>
Median	<u>1</u>	<u>0</u>	<u>-1</u>	<u>1</u>	1	0	1	-2	0	0	1	1	0	1	1	-2

Results: Model with six hours sampling data and **spatialized rainfall**

Cross test (100 NTU threshold overtaking)



	Two branches feed-forward				Two branches recurrent				MLP feed-forward				MLP recurrent			
	F _p	F _n	d _r (6h)	d _d (6h)	F _p	F _n	d _r (6h)	d _d (6h)	F _p	F _n	d _r (6h)	d _d (6h)	F _p	F _n	d _r (6h)	d _d (6h)
T ₂	0	0	-3	2	0	0	3	-3	0	0	2	2	<u>0</u>	<u>0</u>	<u>0</u>	<u>-12</u>
T ₃	<u>0</u>	<u>0</u>	<u>0</u>	<u>0</u>	0	0	1	-2	0	0	1	0	0	1	X	X
T ₆	<u>1</u>	<u>0</u>	<u>-1</u>	<u>0</u>	1	0	1	-1	0	0	3	-1	0	0	2	-2
T ₇	Stop set				0	0	X	X	0	0	X	X	0	0	X	X
T ₁₀	0	0	-1	3	<u>0</u>	<u>0</u>	<u>0</u>	<u>4</u>	0	0	3	3	Stop set			
T ₁₁	1	0	-1/2	-1/1	<u>0</u>	<u>0</u>	<u>0/3</u>	<u>-3/-2</u>	0	0	-2/-3	-1/1	0	1	-1/X	-1/X
T ₁₆	0	0	-1	2	Stop set				<u>0</u>	<u>0</u>	<u>0</u>	<u>1</u>	0	0	1	1
T ₁₇	<u>1</u>	<u>1</u>	<u>2</u>	<u>3</u>	0	3	X	X	Stop set				1	3	X	X
T ₁₈	<u>0</u>	<u>0</u>	<u>X</u>	<u>X</u>	2	0	X	X	<u>0</u>	<u>0</u>	<u>X</u>	<u>X</u>	<u>0</u>	<u>0</u>	<u>X</u>	<u>X</u>
T ₂₂	2	0	X	X	2	0	X	X	<u>0</u>	<u>0</u>	<u>X</u>	<u>X</u>	<u>0</u>	<u>0</u>	<u>X</u>	<u>X</u>
Median	<u>1</u>	<u>0</u>	<u>-1</u>	<u>1</u>	1	0	1	-2	0	0	1	1	0	1	1	-2

Conclusion

Goal of the study:

- 12 hour lead time operational turbidity forecasting
 - Turbidity peak forecasting
 - 100 NTU threshold overtaking forecast

Method:

- Neural network (16 models)
 - Multi-layer Perceptron / Two Branches
 - 1 hour/ 6 hours sampling
 - Recurrent / Feed-forward
 - Mean/spatialized Rainfall

Conclusion

Results:

- Spatialized rainfalls increase the complexity but not the efficiency
- Generally feed forward models are better to forecast the **amplitude** of peaks when recurrent models are better to forecast the **synchronization** of peaks
- The threshold overtaking is predicted with very good efficiency

Future work

- 24 hours lead time forecast
- Multiresolution analysis
- Combine the multilayer perceptron and the two branches to forecast peak and threshold overtaking

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Thank you for your attention

Yport cliffs

Quality criteria

Nash criterion and Percentage Peak Discharge

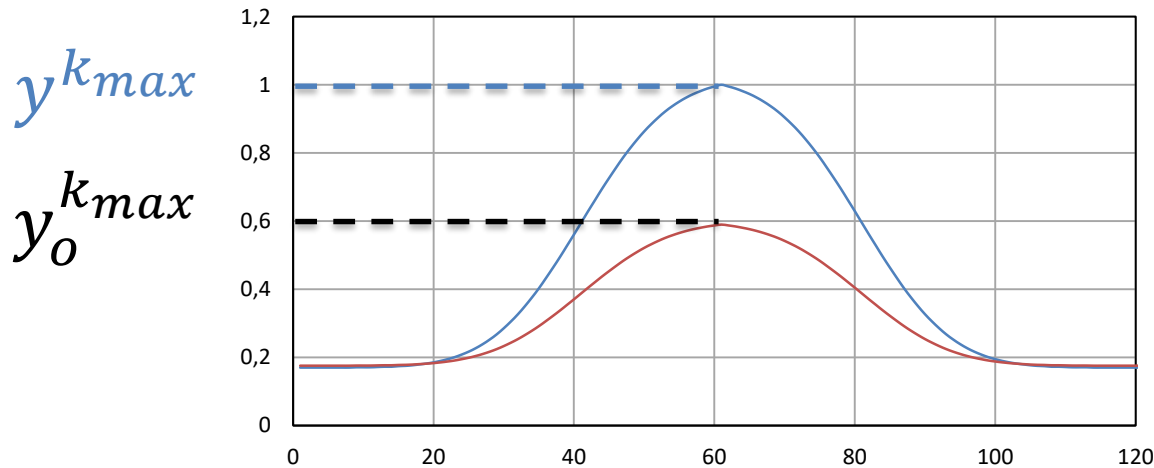
$$R^2 = 1 - \frac{\sum_{k=1}^n (y_o^k - y^k)^2}{\sum_{k=1}^n (y_o^k - \bar{y}_o)^2}$$

Nash Criterion (Ref
Nash)

$$P_{PD} = 100 \frac{y^{k_{max}}}{y_o^{k_{max}}}$$

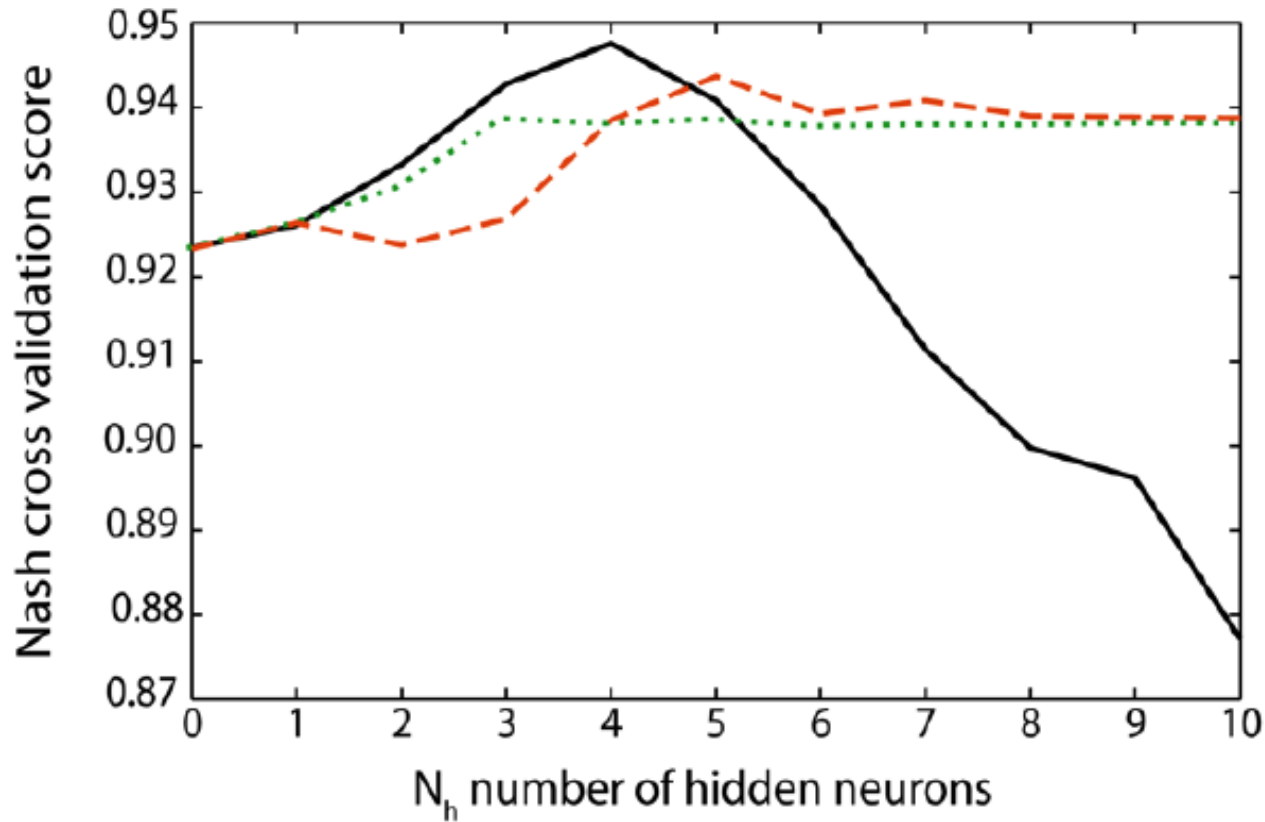
PPD (Percentage
Peak Discharge) (Ref
guillaume article
ness)

Percentage Peak Discharge



Bias variance dilemma

Nash criterion and Percentage Peak Discharge



Kong A. S., & al (2011b)

- Score without regularization method
- - - Score with weight decay
- ... Score with early stopping

Correlations coefficient

	Froberville rainfall	Annouville rainfall	Goderville rainfall	Anglesqueville rainfall	Mannevillette rainfall	Etainhus rainfall
Yport turbidity	0,19	0,20	0,25	0,19	0,21	0,19
Froberville rainfall	1,00	0,50	0,49	0,48	0,38	0,42
Annouville rainfall		1,00	0,59	0,48	0,38	0,46
Goderville rainfall			1,00	0,60	0,42	0,52
Anglesqueville rainfall				1,00	0,48	0,53
Mannevillette rainfall					1,00	0,45
Etainhus rainfall						1,00